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## Disorder and pseudo-symmetry in octakis(trivinylsilyl)octasilicate

Octakis(trivinylsilyl)octasilicate was prepared by capping octaspherosilicate cubes, $\left[\mathrm{Si}_{8} \mathrm{O}_{20}\right]^{8-}$, with trivinylsilyl groups in methanol solution. Crystals grown from $\mathrm{CCl}_{4}$ crystallize in the tetragonal space group $I 4_{1}$. Systematic absences are consistent with the space group $I 4_{1} / a m d$, although the $R_{\text {int }}$ values clearly indicate $4 / \mathrm{m}$ rather than $4 / \mathrm{mmm}$ Laue symmetry. Structure solution and refinement show that the pseudo $a$-glide results from the approximate $m \overline{3} m$ symmetry of the core $\left(\mathrm{Si}_{8} \mathrm{O}_{12}\right) \mathrm{O}_{8}^{8-}$ unit. The positions of the molecules conform to a $\{110\} d$-glide that is broken by the small rotations of all the molecules in the same direction about [001]. Crystals grown from toluene give a diffraction pattern consisting of sharp peaks that can be indexed on the same ca $7200 \AA^{3}$ unit cell, but with $h+k$ even, and $l$ even only. The $l=$ odd layers contain no Bragg spots, but instead exhibit diffuse sheets of intensity. Within the sheets of diffuse scattering are streaks parallel to $\mathbf{r}^{*}=\langle 110\rangle^{*}$ that cross at the $h+k$ odd Bragg positions. This diffuse scattering pattern arises from well ordered rods of molecules parallel to $c$ with frequent faults in the stacking sequence of molecules parallel to $\langle 110\rangle$, with displacement vectors of [00 $\frac{1}{2}$ ].

## 1. Introduction

Polyhedral oligomeric silsequioxane molecules encompass a wide range of closed- and open-shelled organosilicates (Agaskar et al., 1987; Feher \& Blanski, 1990; Feher et al., 1989). The subset of these that are comprised of a cube of eight Si atoms with 12 bridging O atoms and eight terminal O atoms, $\left[\mathrm{Si}_{8} \mathrm{O}_{20}\right]^{8-}$ (Smolin et al., 1979), and capped with a variety of organic groups (Hasegawa et al., 2003) are of considerable interest because of their potential applications as precursors to polymers (Choi et al., 2003; Costa et al., 2001), ceramics (Agaskar, 1992), catalysts (He \& Zhang, 2006), membranes (Asuncion \& Laine, 2007) and other engineering materials (Agaskar, 1989). The $\left[\mathrm{Si}_{8} \mathrm{O}_{20}\right]^{8-}$ core has dimensions of approximately 0.5 nm per side, and when each corner is capped with a small organic group such as $\mathrm{Si}\left(\mathrm{CH}_{3}\right)_{3}$ the overall dimension is approximately 1 nm per side. Such functionalized $\left[\mathrm{Si}_{8} \mathrm{O}_{20}\right]^{8-}$ molecules are thus excellent precursors to nanostructured materials (Laine, 2005; Tamaki et al., 2001, 2003; Waddon \& Coughlin 2003; Zheng et al., 2002). The title compound, octakis(trivinylsilyl)octasilicate, $\quad\left[\mathrm{Si}\left(\mathrm{C}_{2} \mathrm{H}_{3}\right)_{3}\right]_{8}{ }_{8}$ [ $\mathrm{Si}_{8} \mathrm{O}_{20}$ ], has the maximum number of vinyl groups on each cube vertex possible in the first generation of a modified cube. Such hyper-functionalized polyhedra are rare and offer unique opportunities for further modification and materials synthesis.

Octakis(trivinylsilyl)octasilicate was prepared by a modification of the method of Hoebbel for the preparation of capped $\left[\mathrm{Si}_{8} \mathrm{O}_{20}\right]^{8-}$ materials (Hoebbel et al., 1982). Tetra-

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methylorthosilicate and tetramethylammonium hydroxide were mixed in methanol to form the cubic $\left[\mathrm{Si}_{8} \mathrm{O}_{20}\right]^{8-}$ silica core, followed by the addition of trivinylchlorosilane to cap the vertices of the cube (Fig. 1). Crystals were subsequently grown under two different conditions, giving two different, but geometrically related, unit cells. This paper describes the process of solving and refining both of these structures, as an illustration of both pseudo-symmetry and how the structure of a well ordered molecular compound can be used to determine the average structure of its disordered variant.

## 2. Experimental

Colorless plates were crystallized by slow evaporation of either $\mathrm{CCl}_{4}$ (cs521) or toluene (cs511) at room temperature. Diffraction data were collected with an Oxford Diffraction Xcalibur diffractometer equipped with a Sapphire 2 CCD detector and Mo $K \alpha(\lambda=0.71073 \AA)$ radiation, operating at 50 kV and 40 mA . The data-collection routines, unit-cell refinements and data processing were carried out with the program CrysAlis (Oxford Diffraction, 2004). The structures were solved by direct methods and refined using SHELXTL $N T$ (Sheldrick, 2008), which was also used for molecular graphics generation. Non-H atoms were refined anisotropically and a riding model was used for the H atoms. The final refinement of cs521 included a merohedral twin model for inversion [Flack parameter $=0.59$ (13)]. The inability to model a small degree of short-range disorder, evident by a small amount of diffuse scattering parallel to $\mathbf{r}^{*}=\langle 110\rangle^{*}$, is presumably the cause of the slightly unsatisfactory displacement parameters and residual electron density. The final
$\mathrm{Si}\left(\mathrm{OCH}_{3}\right)_{4}+\left(\mathrm{CH}_{3}\right)_{4} \mathrm{NOH} \xrightarrow{\mathrm{CH}_{3} \mathrm{OH}}\left[\mathrm{Si}_{3} \mathrm{O}_{20}\right]^{3-}$


Figure 1
Synthetic scheme for octakis(trivinylsilyl)octasilicate.
refinement of cs511 included a whole-molecule disorder model that is described in detail below.

## 3. Results and discussion

### 3.1. Crystal structure of cs521

Initial screening of the cs521 crystals grown from $\mathrm{CCl}_{4}$ was very promising. Diffraction peaks were clean and single and the preliminary unit-cell parameters were consistent with a body-centered tetragonal lattice with $V=7197 \AA^{3}$ (hereafter referred to as the $7200 \AA^{3}$ cell) and $Z=4$. Apparent systematic absences suggested $I 4_{1} / a m d$ space-group symmetry - a space group that was clearly ruled out by the $4 / m$ Laue symmetry of the diffracted intensities ( $R_{\text {int }} 4 / \mathrm{m}=0.08 ; R_{\text {int }} 4 / \mathrm{mmm}=0.48$ ). Assuming that the apparent $d$-glide resulted from pseudosymmetry, we attempted to solve the structure in $I 4_{1} / a$ with the molecule centered at Wyckoff positions $4(a)$ or $4(b)$ of $\overline{4}$ point symmetry (as required by $Z=4$ ). The structure solution obtained in $I 4_{1} / a$ was not satisfactory. The $\left[\mathrm{Si}_{8} \mathrm{O}_{20}\right]^{8-}$ core could be identified, but the trivinylsilyl arms were disordered and appeared to adopt chemically and sterically unreasonable conformations. The space group $I 4_{1}$ gave a satisfactory solution. Crystallographic details for cs521 are presented in Table $1 .{ }^{1}$

In space group $I 4_{1}$, the asymmetric unit of the structure comprises half of the molecule; the molecules are centered at Wyckoff position 4(a) of multiplicity 4 and the point symmetry 2 generates the other half of each molecule. The $c$ axis of the unit cell is one molecule high and the $a$ and $b$ axes are each 2 molecules wide, giving approximate molecular dimensions $\frac{1}{2} a \times \frac{1}{2} a \times c\left(10.585 \times 10.585 \times 16.059 \AA^{3}\right)$, and a molecular volume of $1799.30 \AA^{3}$. The individual molecules in the unit cell are related by the $4_{1}$ and $4_{3}$ axes. The floating $z$ coordinate in space group $I 4_{1}$ was intentionally chosen so that molecules are centered at $000, \frac{1}{2} \frac{1}{2} \frac{1}{2}, 0 \frac{1}{2} \frac{1}{4}$ and $\frac{1}{2} 0 \frac{3}{4}$. The final refinement for cs521 included a twin model for inversion; the Flack parameter refined to 0.59 (13) so, within uncertainties, the crystal consists of an equal number of both twin orientations. Note that the imposition of an inversion twin on space group $I 4_{1}$ amounts to interchange of the screw axes, such that the $4_{1}$ axes become $4_{3}$ and the $4_{3}$ axes become $4_{1}$, and thus interchange of the $z$ coordinate of the molecule centroids at $0 \frac{1}{2} z$ and $\frac{1}{2} 0 z$, from $z=\frac{1}{4}$ to $z=\frac{3}{4}$, and $z=\frac{3}{4}$ to $z=\frac{1}{4}$ respectively (Fig. 2c).

The molecular-point symmetry 2 is dictated by both the trivinylsilyl arms and the $\mathrm{Si}_{8} \mathrm{O}_{12}$ core. The $\mathrm{Si}_{8} \mathrm{O}_{12}$ core approximates $m \overline{3} m$ point symmetry. The molecular symmetry is reduced to tetragonal point symmetry $4 / m$ by the average $\mathrm{Si}_{\text {core }}-\mathrm{O}-\mathrm{Si}_{\text {arm }}$ angle of $147(4)^{\circ}$ (Table 2) with all eight trivinylsilyl arms rotated towards the $c$ axis. This makes the molecule substantially longer in the $z$ dimension (Fig. 2a). Mirror symmetry parallel to (001) is broken by further distortion of the trivinylsilyl arms so they are not superimposed when viewed in projection down the $c$ axis (Fig. 2b).

[^2]Table 1
Experimental details.

|  | cs521 | cs511 |
| :---: | :---: | :---: |
| Crystal data |  |  |
| Crystallization solvent | $\mathrm{CCl}_{4}$ | Toluene |
| Chemical formula | $\mathrm{C}_{48} \mathrm{H}_{72} \mathrm{O}_{20} \mathrm{Si}_{16}$ | $\mathrm{C}_{48} \mathrm{H}_{72} \mathrm{O}_{20} \mathrm{Si}_{16}$ |
| $M_{r}$ | 1418.50 | 1418.50 |
| Cell setting, space group | Tetragonal, $I 4_{1}$ | Tetragonal, 14 |
| Temperature (K) | 100 (2) | 100 (2) |
| $a, ~ c(\AA)$ | 21.1698 (18), 16.059 (3) | 15.0040 (6), 7.9872 (5) |
| $V\left(\AA^{3}\right)$ | 7197.2 (16) | 1798.08 (15) |
| $Z$ | 4 | 1 |
| $D_{x}\left(\mathrm{Mg} \mathrm{m}^{-3}\right)$ | 1.309 | 1.311 |
| Radiation type | Mo K $\alpha$ | Mo $K \alpha$ |
| $\mu\left(\mathrm{mm}^{-1}\right)$ | 0.35 | 0.35 |
| Crystal form, color | Plate, colorless | Plate, colorless |
| Crystal size (mm) | $0.12 \times 0.11 \times 0.04$ | $0.16 \times 0.16 \times 0.06$ |
| Data collection |  |  |
| Diffractometer | Oxford Diffraction Xcalibur2 | Oxford Diffraction Xcalibur2 |
| Data collection method | $\varphi$ and $\omega$ scans, 50 s per frame | $\varphi$ and $\omega$ scans, 25 s per frame |
| Absorption correction | None | None |
| No. of measured, independent and observed reflections | 26 352, 10 566, 6414 | 10 423, 1399, 1394 |
| Criterion for observed reflections | $I>2 \sigma(I)$ | $I>2 \sigma(I)$ |
| $R_{\text {int }}$ | 0.052 | 0.056 |
| $\theta_{\text {max }}\left({ }^{\circ}\right)$ | 30.1 | 30.1 |
| No. and frequency of standard reflections | 2 every 50 frames | 2 every 50 frames |
| Intensity decay (\%) | $<2$ | $<2$ |
| Refinement |  |  |
| Refinement on | $F^{2}$ | $F^{2}$ |
| $R\left[F^{2}>2 \sigma\left(F^{2}\right)\right], w R\left(F^{2}\right), S$ | $0.060,0.137,0.96$ | 0.061, 0.152, 1.23 |
| No. of reflections | 10566 | 1399 |
| No. of parameters | 380 | 190 |
| H -atom treatment | Constrained to parent site | Constrained to parent site |
| Weighting scheme | $\begin{aligned} & w=1 /\left[\sigma^{2}\left(F_{o}^{2}\right)+(0.0571 P)^{2}\right], \text { where } \\ & \quad P=\left(F_{o}^{2}+2 F_{c}^{2}\right) / 3 \end{aligned}$ | $\begin{aligned} & w=1 /\left[\sigma^{2}\left(F_{o}^{2}\right)+(0.0665 P)^{2}+\right. \\ & 1.9447 P], \text { where } P=\left(F_{o}^{2}+2 F_{c}^{2}\right) / 3 \end{aligned}$ |
| $(\Delta / \sigma)_{\text {max }}$ | 0.001 | <0.0001 |
| $\Delta \rho_{\text {max }}, \Delta \rho_{\text {min }}\left(\mathrm{e} \AA^{-3}\right)$ | 1.15, -0.33 | 0.34, -0.29 |
| Absolute structure | Flack (1983), 5098 Friedel pairs | NA, Friedels merged |
| Flack parameter | 0.59 (13) | NA |
| Rogers parameter | < 2 \% | NA |

Computer programs used: CrysAlis (Oxford Diffraction, 2004), SHELXL97 (Sheldrick, 2008).

Wyckoff position 4(a) (origin choice 1) with $\overline{4} m 2$ symmetry. In addition to the distortion of the molecule breaking the $\overline{4} m 2$ symmetry, the orientation of the molecules in the unit cell, such that every molecule is rotated clockwise ca $6.6^{\circ}$ about [001], breaks the $\overline{4} m 2$ symmetry (Fig. 2). This rotation also breaks both the . $m$. and .. $d$ symmetry associated with $I 4_{1} / a m d$.

### 3.2. Diffuse scattering in cs511

The cs511 crystals grown from toluene give raw diffraction images with sharp peaks (i.e. Bragg reflections) and streaks of diffuse scattering halfway between the Bragg reflections (Fig. 3a). The Bragg reflections can be indexed on the same $7200 \AA^{3}$ unit cell as cs521, but all have indices $h+k=$ even and $l=$ even. When cs511 is indexed to the $7200 \AA^{3}$ cell, diffuse scattering occurs as two-dimensional sheets in the $l=$ odd planes. These sheets of intensity are consistent with well ordered rods of molecules parallel to $c$, but adjacent rods that are 'randomly' displaced by faults with a displacement vector of $\left[00 \frac{1}{2}\right]$. Within the sheets of diffuse scattering, the intensity is not uniform. There are higher intensity streaks parallel to $\mathbf{r}^{*}=\langle 110\rangle^{*}$ that cross and form diffuse maxima at $h+k=$ odd Bragg positions (Fig. 3b). These streaks indicate additional ordering of the rods of molecules to form ordered $\{110\}$ sheets within the crystal. Complete ordering in this fashion would lead to the development of Bragg reflections at the intersection of the streaks at $h+k=$ odd and $l=$ odd positions, and hence the I lattice, as found in the cs521 crystals. In cs511, however, the ordering is interrupted by [00 $\frac{1}{2}$ ] displacements at faults between neighboring $\{110\}$ sheets and this results in the streaks in the diffraction pattern (Fig. 3b).

### 3.3. Crystal structure of cs511

The Bragg spots of cs511 represent the average disordered unit cell, taking into consideration the faults described above. Indexing the Bragg reflections of cs511 gives a unit cell of $V=$ 1798.08 (15) $\AA^{3}$ (herein referred to as 'the $1800 \AA^{3}$ cell') that is geometrically related to 'the $7200 \AA^{3}$ cell' of cs521. The transformations between the $7200 \AA^{3}$ cell and the $1800 \AA^{3}$ cell are described in Table 3 and depicted in Fig. 4(a). Table 4


Figure 2
(a) Displacement ellipsoid drawing (50\%) of cs521 viewed down [100] and depicting the dimensions of the molecule. (b) View down [001] depicting the distortions of the $\mathrm{Si}_{8} \mathrm{O}_{12}$ core and the trivinylsilyl arms that reduce the molecular point symmetry to 2. (c) Packing diagram overlaid on a symmetry diagram for $I 4_{1}$ with pseudo $a \ldots, m$. and $\ldots d$ symmetry elements shown in green. Vinyl groups are omitted for clarity. The $z$ coordinates of the molecule centroids are given in black. The inversion twin in $I 4_{1}$ amounts to interchange of the screw axes, such that the $4_{1}$ axes become $4_{3}$ and the $4_{3}$ axes become $4_{1}$.

Table 2
Average bond lengths $(\AA)$ and angles $\left({ }^{\circ}\right)$ for cs521 and cs511.

|  | cs521 |  | cs511 |  |
| :---: | :---: | :---: | :---: | :---: |
|  | Bond direction $\dagger$ | Average | Bond direction | Average |
| $\mathrm{Si}_{\text {core }}-\mathrm{O}_{\text {core }}$ | $\\|\langle 100\rangle$ | 1.607 (4) | - | 1.608 (8) |
| $\mathrm{Si}_{\text {core }}-\mathrm{O}_{\text {core }}$ | $\\|\langle 010\rangle$ | 1.611 (7) | - | - |
| $\mathrm{Si}_{\text {core }}-\mathrm{O}_{\text {core }}$ | $\\|\langle 001\rangle$ | 1.606 (10) | - | 1.607 (14) |
| $\mathrm{Si}_{\text {core }}-\mathrm{O}_{\text {core }}$ | - | 1.588 (8) | $\\|\langle 110\rangle$ | 1.591 (1) |
| $\mathrm{O}_{\text {arm }}-\mathrm{Si}_{\text {arm }}$ | - | 1.643 (8) | - | 1.628 (1) |
| $\mathrm{Si}_{\text {arm }}-\mathrm{C}$ | - | 1.846 (10) | \|| $\langle 001\rangle$ | 1.838 (9) |
| $\mathrm{CH}=\mathrm{CH}_{2}$ | - | 1.320 (20) | - | 1.29 (3) |
| Si . . Si edge | \\| $\langle 100\rangle$ | 3.105 (11) | - | 3.089 (4) |
| Si . . Si edge | $\\|\langle 010\rangle$ | 3.063 (15) | - | - |
| Si . . Si edge | $\\|\langle 001\rangle$ | 3.115 (5) | - | $3.110 \ddagger$ |
| $\mathrm{Si} \cdots$ Si face diagonal | $\perp\langle 100\rangle$ | 4.37 (3) | $\\|\langle 110\rangle$ | 4.38 (2) |
| Si $\ldots$ Si face diagonal | $\perp\langle 010\rangle$ | 4.40 (2) | - | - |
| Si . . Si face diagonal | $\pm\langle 001\rangle$ | 4.361 (6) | \\| $\langle 001\rangle$ | 4.37 (3) |
| Si $\cdots$ Si body diagonal | - | 6.359 (2) | $\perp\langle 110\rangle$ | $5.262 \ddagger$ |
| $\mathrm{Si}_{\text {core }}-\mathrm{O}_{\text {core }}-\mathrm{Si}_{\text {core }}$ | $\\|\langle 100\rangle$ | 150.1 (11) | - | 147.7 (15) |
| $\mathrm{Si}_{\text {core }}-\mathrm{O}_{\text {core }}-\mathrm{Si}_{\text {core }}$ | $\\|\langle 010\rangle$ | 143.7 (13) | $\perp\langle 001\rangle$ | - |
| $\mathrm{Si}_{\text {core }}-\mathrm{O}_{\text {core }}-\mathrm{Si}_{\text {core }}$ | \\| $\langle 001\rangle$ | 151.7 (2) | - | 150.7 $\ddagger$ |
| $\mathrm{Si}_{\text {core }}-\mathrm{O}_{\text {core }}-\mathrm{Si}_{\text {arm }}$ | - | 147 (4) | $\\|\langle 110\rangle$ | 147 (4) |
| $\mathrm{O}_{\text {core }}-\mathrm{Si}_{\text {core }}-\mathrm{O}_{\text {core }}$ | - $\langle 100\rangle$ | 109.3 (7) | - | 109.4 (8) |
| $\mathrm{O}_{\text {core }}-\mathrm{Si}_{\text {core }}-\mathrm{O}_{\text {core }}$ | $\perp\langle 010\rangle$ | 109.5 (9) | $\\|\langle 001\rangle$ | - |
| $\mathrm{O}_{\text {core }}-\mathrm{Si}_{\text {core }}-\mathrm{O}_{\text {core }}$ | $\pm\langle 001\rangle$ | 109.4 (2) | - | 109.2 (7) |
| $\mathrm{O}_{\text {core }}-\mathrm{Si}-\mathrm{O}_{\text {arm }}$ | $\\|\langle 100\rangle$ | 109.9 (9) | - $\langle 110\rangle$ | 110.4 (14) |
| $\mathrm{O}_{\text {core }}-\mathrm{Si}-\mathrm{O}_{\text {arm }}$ | $\\|\langle 010\rangle$ | 110.1 (10) | - | - |
| $\mathrm{O}_{\text {core }}-\mathrm{Si}-\mathrm{O}_{\text {arm }}$ | $\\|\langle 001\rangle$ | 108.6 (7) | $\perp\langle 001\rangle$ | 108.1 (6) |
| $\mathrm{O}_{\text {arm }}-\mathrm{Si}_{\text {arm }}-\mathrm{C}$ | - | 108.0 (11) | $\\|\langle 110\rangle$ | 107.6 (14) |
| $\mathrm{C}-\mathrm{Si}-\mathrm{C}$ | - | 110.9 (13) | - | 111.3 (13) |
| $\mathrm{Si}-\mathrm{C}=\mathrm{C}$ | - | 124.6 (14) | $\\|\langle 001\rangle$ | 126 (3) |

$\dagger$ All directions are defined relative to the molecule centered at $\frac{1}{2} \frac{1}{2} 0$ in the $7200 \AA^{3}$ cell. $\ddagger$ There is only one value in this category so the standard uncertainty could not be calculated.
describes the diffuse scattering pattern relative to both cell settings.

The Laue symmetry and systematic absences of cs511 in the $1800 \AA^{3}$ cell are consistent with space groups $I 4 / m, I \overline{4}$ or $I 4$ and $Z=1$. A value of $Z=1$ is not reasonable for a tetragonal I lattice unless there is whole-molecule disorder with equivalent positions at $0,0,0+$ and $\frac{1}{2}, \frac{1}{2} \frac{1}{2}+$, each of $50 \%$ occupancy. Fortunately, whole-molecule disorder is consistent with the observed diffuse scattering pattern in cs511. In the ensuing discussion we begin with the ordered cs521 structure in the $7200 \AA^{3}$ cell, apply the $\left[00 \frac{1}{2}\right]$ fault vectors on $\{110\}$ fault planes to build a model disordered structure and ultimately obtain a refined structure for cs 511 in the $1800 \AA^{3}$ unit cell.

Fig. $4(b)$ shows a schematic of the cs521 structure overlaid on an $I 4_{1}$ symmetry diagram. Each rectangle represents one $\mathrm{C}_{48} \mathrm{H}_{72} \mathrm{O}_{20} \mathrm{Si}_{16}$ molecule and is intended to emphasize the point symmetry 2 and the non-overlapping trivinylsilyl arms. Although the $z$ coordinates are not crystallographically constrained in $I 4_{1}$, for convenience we have defined the $z$ coordinates so that one of the molecules is centered at the origin. To understand the effect of the faults parallel to $\{110\}$ (depicted in green in Fig. 4b), concentrate on the molecules labelled $A$ and $B$, and centered at $0,0,0$ and $0, \frac{1}{2}, \frac{1}{4}$, respectively. The displacement of $\left[00 \frac{1}{2}\right]$ across the fault causes the centroid
of $A$ to shift to $0,0, \frac{1}{2}$ and the centroid of $B$ to shift to $0, \frac{1}{2}, \frac{3}{4}$. Assuming that, on average across the entire crystal, the faults cause $50 \%$ disorder, the average structure has the $A$ molecules centered at $0,0,0$ and $\frac{1}{2}$, and the $B$ molecules centered at $0, \frac{1}{2}, \frac{1}{4}$ and $\frac{3}{4}$, each with $50 \%$ occupancy. Applying the $\left[00 \frac{1}{2}\right]$ fault vector to all of the molecules in the unit cell generates the average structure shown in Fig. 4(c). Since the environments

(a)

(b)

Figure 3
(a) Sample CCD image showing the diffuse scattering halfway between Bragg reflections. (b) The $h k 5$ layer illustrating the crisscross pattern of diffuse scattering present at the $h k l, l=$ odd layers of the $7200 \AA^{3}$ cell.

Table 3
Transformations from the $7200 \AA^{3}$ cell to the $1800 \AA^{3}$ cell.

| $a$ | $a_{1800}=1 / 2^{1 / 2} a_{7200}$ |
| :---: | :---: |
| c | $c_{1800}=\frac{1}{2} c_{7200}$ |
| V | $V_{1800}=\frac{1}{4} V_{7200}$ |
| Transformation matrices | $\mathbf{T}=\left(\begin{array}{ccc}\frac{1}{2} & \frac{1}{2} & 0 \\ -\frac{1}{2} & \frac{1}{2} & 0 \\ 0 & 0 & \frac{1}{2}\end{array}\right) \mathbf{T}^{-1}=\left(\begin{array}{ccc}1 & -1 & 0 \\ 1 & 1 & 0 \\ 0 & 0 & 2\end{array}\right)$ |
| Unit-cell dimensions | $(a b c)_{1800}=(a b c)_{7200} \mathbf{T}$ |
| Miller indices | $(h k l)_{1800}=(h k l)_{7200} \mathbf{T}$ |
| Atomic coordinates | $\left(\begin{array}{l}x \\ y \\ z\end{array}\right)_{1800}=\mathbf{T}^{-1}\left(\begin{array}{l}x \\ y \\ z\end{array}\right)_{7200}$ |

Table 4
Description of the diffuse scattering pattern in cs511 relative to the $7200 \AA^{3}$ and $1800 \AA^{3}$ unit cells.

|  | $7200 \AA^{3}$ cell | $1800 \AA^{3}$ cell |
| :--- | :--- | :--- |
| $a, c(\AA)$ | $21.1698(18), 16.059(3)$ | $15.0040(6), 7.9872(5)$ |
| Indices of Bragg | $h k l, h+k=$ even, | $h k l, h+k+l=$ even |
| reflections | $\quad l=$ even | $($ I lattice $)$ |
| Diffuse scattering | Sheets in $l=$ odd layers <br>  <br>  <br>  <br>  <br>  <br> Streaks $\\| \mathbf{r}^{*}=\langle 110\rangle^{*}$ | Sheets in $l=n+\frac{1}{2}$ layers <br>  <br> Streaks cross at <br>  <br> Streaks $\\| \mathbf{r}^{*}=\langle 100\rangle^{*}$ <br> Fault vector |

at $0,0,0.0$ and $0,0, \frac{1}{2}$ are now identical, the unit cell is now best represented by halving the $c$ axis and fixing the occupancies at $50 \%$ (Fig. 4d). Further examination of the model in Fig. 4(d) shows that all of the molecules labeled ' $A$ ' now have exactly equivalent environments, and the cell has become C -face centered. Transformation of this cell to a primitive setting yields the $1800 \AA^{3}$ unit cell (blue cell in Fig. $4 d$ ) obtained from the Bragg reflections of the diffraction pattern for cs511. In this $1800 \AA^{3}$ cell, $A$ is centered at $0,0,0$ and $B$ is centered at $\frac{1}{2}, \frac{1}{2}, \frac{1}{2}$, each with $50 \%$ occupancy. Also, the original $4_{1}$ axes of the $7200 \AA^{3}$ unit cell become $4_{2}$ axes in the disordered $1800 \AA^{3}$ cell and the space group becomes $P 4_{2}$.

Recall that the Bragg reflections in cs511 are consistent with space groups $I 4, I \overline{4}$ or $I 4 / \mathrm{m}$. In the current model (Fig. 4d), Ilattice symmetry is broken because $A$ and $B$, although sitting at $0,0,0$ and $\frac{1}{2}, \frac{1}{2}, \frac{1}{2}$, have different orientations; $B$ is rotated $90^{\circ}$ relative to $A$. To obtain $I 4, I \overline{4}$ or $I 4 / m$ from $P 4_{2}$, the molecular point symmetry must be increased to $4, \overline{4}$ or $4 / m$, respectively. Assuming only minor distortions, these three point groups are all compatible with the $\mathrm{Si}_{8} \mathrm{O}_{12}$ core. When considering the relative orientations of the trivinylsilyl arms, however, only point group 4 is reasonable ( $\mathrm{Fig} .5 b$ ). In a projection of the structure of cs521 down [001], note that the $\mathrm{O}_{\mathrm{arm}}-\mathrm{Si}_{\text {arm }}$ atoms do not overlay perfectly and that all the upper $\mathrm{O}_{\text {arm }}-\mathrm{Si}_{\text {arm }}$ atoms are rotated in the same direction relative to the bottom $\mathrm{O}_{\mathrm{arm}}-\mathrm{Si}_{\text {arm }}$ atoms (Fig. 5a). Thus, $4 / m$ symmetry is not compatible with a molecular structure derived from that of cs521 unless there is significant rotation of the arms to bring the upper and lower arms into coincidence in this projection (Fig. 5c). Imposition of point symmetry $\overline{4}$ onto the molecule inherited from cs521 requires a reversal of the relative rota-
tions of upper and lower arms, as indicated in Fig. 5(d). By contrast, point-group symmetry 4 preserves the arrangement of the arms from the structure of cs521 and only has the effect of making some symmetrically equivalent (Fig. 5b). Therefore, the space group $I 4$ was chosen for cs511.

The point symmetry 4 could be imposed on the molecule by one of two methods:
(i) by increasing the point symmetry of the molecule from 2 to 4 (Fig. 6a) or
(ii) by assuming the molecule is of point symmetry 2, but with a $90^{\circ}$ rotational disorder about [001] (Fig. 6b).
The simpler model of increasing the point symmetry of the molecule to 4 was chosen for the first modeling attempt (Fig. $6 a$ ). The following steps were used to derive a model for cs511 from the cs521 solution:
(i) The atomic coordinates from cs521 were transformed to the correct coordinates for the $1800 \AA^{3}$ cell using the transformation matrix shown in Table 3.
(ii) The effect of the $\left[00 \frac{1}{2}\right]$ fault vectors (relative to the $7200 \AA^{3}$ cell) was accounted for by constraining the occupancies at each general position to $50 \%$.
(iii) The molecular point symmetry was increased from 2 to 4. The higher symmetry reduced the number of symmetrically unique atoms from 42 to 21 and the atomic coordinates were averaged accordingly to obtain a starting model.

In this final model, molecules are centered at Wyckoff position 2(a), with the floating $z$ coordinate chosen so that the molecule is centered at $0,0,0$. Note that this effectively places two molecules in the unit cell at $0,0,0$ and at $\frac{1}{2}, \frac{1}{2}, \frac{1}{2}$, but since the occupancies are constrained to $50 \%, Z=1$ in this bodycentered lattice.

Refining this model to the Bragg reflections of the $1800 \AA^{3}$ cell was very successful, giving $R 1$ and $w R 2$ values similar to the ordered model (Table 1). Average bond lengths and angles are given in Table 2. Fig. 7(a) shows the displacement ellipsoid drawing. The packing diagram (Fig. 7b) illustrates the fourfold symmetry of the molecule, the $c a 6.6^{\circ}$ rotation of the molecule and the I4 spacegroup symmetry. There are only very small changes in the molecular geometry between this structure and that of cs521, despite the imposition of higher point symmetry (Table 2). At this point we revisited the possibility that the space group could be $I 4 / m$, which requires molecular point symmetry $4 / m$. The packing diagram down b (Fig. 7b) clearly demonstrates that the trivinylsilyl arms do not overlap and thus there is no mirror symmetry perpendicular to [001].

Now, consider the diffuse scattering relative to the $1800 \AA^{3}$ cell (Table 4). The sheets of diffuse scattering are in the $l=n+\frac{1}{2} \quad$ layers $\quad$ with streaks parallel to $\mathbf{r}^{*}=$ $\langle 100\rangle^{*}$ that cross at the $h+\frac{1}{2}, k+\frac{1}{2}$ Bragg positions. Thus, relative to the $1800 \AA^{3}$ cell, the disorder in the stacking sequence of the molecules is along the $\langle 100\rangle$ directions with a fault vector of [001]. Fig. 7(c) depicts the average

Figure 4
(a) Geometric relation between the $7200 \AA^{3}$ cell of cs521 (black) and the $1800 \AA^{3}$ cell of cs511 (blue). The fault planes (green dotted lines) lie parallel to $\{110\}$ in the $7200 \AA^{3}$ cell, equivalent to $\{100\}$ in the $1800 \AA^{3}$ cell. (b) Fault planes overlaid on a schematic of the cs521 structure and depicting $\{110\}$ fault planes with $00 \frac{1}{2}$ displacement across the faults. Each 'armed rectangle' is an exaggerated representation of the point symmetry 2 of the molecule. (c) Average structure overlaid on the $7200 \AA^{3}$ cell and assuming $50 \%$ disorder caused by the $00 \frac{1}{2}$ fault. (d) Average structure overlaid on the $1800 \AA^{3}$ cell (blue) and the $7200 \AA^{3}$ cell (black). There is $50 \%$ occupancy at each site. The symmetry elements correspond to the space group $P 4_{2}$ for the $1800 \AA^{3}$ cell.

(a)

(c)

(b)
ac

$$
\underset{i}{x / 2}
$$

(d)
(a)

(c)

X
(d)


Figure 5
An exaggerated schematic representation of possible (but exaggerated) $\mathrm{Si}_{8} \mathrm{O}_{12}$ core symmetries and orientations of the trivinylsilyl arms, as viewed down [001]. Upper trivinylsilyl arms are solid; lower arms are dashed. (a) In the cs521 model of point symmetry 2, all upper arms are rotated in the same direction compared with the lower arms. (b) Increasing the symmetry from 2 to 4 maintains the topology of the trivinylsilyl arms. (c) Increasing the symmetry to $4 / m$ requires significant distortion so that the upper and lower arms overlay. (d) Increasing the symmetry to $\overline{4}$ requires a change in arm topology, with alternate upper arms rotated in opposite directions.


Figure 6
Two possible models that generate a disordered structure with $I 4$ symmetry. (a) Molecular point symmetry is increased from 2 to 4 . There is a $50 \%$ occupancy at each site. (b) The molecule is disordered via a $90^{\circ}$ rotation about [001]. The occupancy of each position is $25 \%$.
structure that results from frequent faulting, with apparent interpenetration of adjacent molecules along [001]. This structure is to be interpreted as having a molecule residing at either $z=1,3,5, \ldots$ or $z=2,4,6, \ldots$, therefore, on average,


Figure 7
Final model refined to the Bragg reflections for the diffuse scattering sample. (a) Displacement ellipsoid drawing at $50 \%$ probability. H atoms are omitted for clarity. (b) Packing diagram viewed down [001]. (c) View along [001] illustrating the disorder resulting from the [001] fault vectors (relative to cs511).
molecules are centered at $z=1,2,3, \ldots$, each $50 \%$ of the time and $2,4,6, \ldots$, each $50 \%$ of the time.

## 4. Conclusions

Crystals of $\mathrm{C}_{48} \mathrm{H}_{72} \mathrm{O}_{20} \mathrm{Si}_{16}$ have been grown from toluene and $\mathrm{CCl}_{4}$. It is not clear whether the crystallization solvent determines the structure or whether other subtle differences such as speed of crystallization caused the molecule to crystallize in two different, but related, forms. In the two structures the molecular geometry and the packing differ only slightly, as evidenced by the ability to use the solution from cs521 to calculate the preliminary model for cs511. The structures do differ in the formal point symmetry of the molecules. The molecule in cs521 has point symmetry 2 , while the molecule in cs511 has apparent point symmetry 4. It is unclear, and most likely impossible to determine, if the 4 symmetry of cs511 results from $90^{\circ}$ rotational disorder of molecules with point symmetry 2 or from the molecules adopting true point symmetry 4. For simplicity, we chose to constrain the cs511 molecule to point symmetry 4 and thereby avoid modelling additional disorder.

The major difference between the two crystal forms is therefore the frequency of the faults within the crystals. In cs521, a twin model successfully reproduced the measured intensity data. To understand this, consider that the [00 $\left.\frac{1}{2}\right]$ fault vectors effectively reverse the direction of the $4_{1}$ and $4_{3}$ screw axes (Fig. $4 b$ ). The same reversal of the $4_{1}$ and $4_{3}$ screw axes can be obtained by imposition of an inversion twin operation. Therefore, inversion twinning cannot be structurally distinguished from the effect of an isolated fault plane. However, the implicit assumption within a twin model is that there is no significant coherent diffraction from adjacent domains related by the twin operation, and therefore the overall intensity is a function of the sum of the squares of the structure factors, $I(h k l)_{\text {obs }} \propto x F(h k l)_{1}^{2}+(1-x) F(h k l)_{2}^{2}$, where the Flack parameter, $x$, is the fraction of the intensity contribution from each twin. In cs521 the Flack parameter refined to 0.59 (13), indicating approximately equal proportions of the two twin orientations or domains. The success of the twin model to reproduce the measured intensity data indicates that there is long-range order in cs521, and thus that the distance between fault planes is relatively large compared with the coherence
length of X-rays. In cs511 the faults are much more frequent, as indicated by the strong diffuse scattering. In this case, the total scattering comes from the coherent scattering from adjacent domains. The intensity of the Bragg reflections is a function of the square of the sum of the structure factors, i.e. $I(h k l)_{\text {obs }} \propto\left[\frac{1}{2} F(h k l)_{1}+\frac{1}{2} F(h k l)_{2}\right]^{2}$, and the intensity data are modelled as a single disordered structure. Thus, both crystal forms are almost identical, except that they differ in the frequency of the faults or, equivalently, the size of the ordered domains of molecules.

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